

(*****
Saturated structures: Expected number of base pairs.

From DSV

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Clear["P", "S", "R"]
g1 = -S + z + z^2 + zR + z^2R + uz^2S + uz^2S^2;
g2 = -R + uz^2S + uz^2RS;
P = Resultant[-S + z + z^2 + zR + z^2R + uz^2S + uz^2S^2, -R + uz^2S + uz^2RS, R]
P = Suz^2 (z + z^2) - (-1 + Suz^2) (-S + z + z^2 + Suz^2 + S^2 uz^2)
dPdS = Simplify[D[P, S]]
dPdS = -1 + (1 + 4 S) uz^2 - S (2 + 3 S) u^2 z^4
dPdu = Simplify[D[P, u]]
dPdu = S z^2 (1 - 2 S^2 u z^2 + S (2 - 2 u z^2))
S = T + K Sqrt[X];
denom =
Series[(-1 + (1 + 4 S) (rho - rho X)^2 - S (2 + 3 S) (rho - rho X)^4), {X, 0, 1}] /. X -> (1 - z / rho)

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(*****
This produces an expansion of "denom" as follows
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$$\text{denomApprox} = (4K\rho^2 - 2K\rho^4 - 6K\rho^4T) \sqrt{1 - \frac{z}{\rho}}$$

(*****
Compute numerator in limit as "S,z" approach "T,rho"
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K = -3.808190403387938`
T = 1.6568963314781193`
rho = 0.4246873104202721`
numer = Expand[S z^2 (1 - 2 S^2 z^2 + S (2 - 2 z^2))]
numer /. {S -> 1.6568963314781193, z -> rho} = 0.8145799335195365`;

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(*****
Compute denominator in limit as "S,z" approach "T,rho"
*****)

K = -3.808190403387938`
T = 1.6568963314781193`
rho = 0.4246873104202721`
A = factorOfDenom = (4 K rho² - 2 K rho⁴ - 6 K rho⁴ T) = 1.268090901429324`
B = 1 / A = -0.78858700024805473