

# Boltzmann probability of RNA structural neighbors and riboswitch detection

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## ABSTRACT

**Motivation:** We describe algorithms implemented in a new software package, RNABOR, to investigate structures in a neighborhood of an input secondary structure  $S$  of an RNA sequence  $s$ . The input structure could be the minimum free energy structure, the secondary structure obtained by analysis of the X-ray structure or by comparative sequence analysis, or an arbitrary intermediate structure.

**Results:** A secondary structure  $T$  of  $s$  is called a  $\delta$ -neighbor of  $S$  if  $T$  and  $S$  differ by exactly  $\delta$  base pairs. RNABOR computes the number ( $N^\delta$ ), the Boltzmann partition function ( $Z^\delta$ ) and the minimum free energy ( $MFE^\delta$ ) and corresponding structure over the collection of all  $\delta$ -neighbors of  $S$ . This computation is done simultaneously for all  $\delta \leq m$ , in run time  $O(mn^3)$  and memory  $O(mn^2)$ , where  $n$  is the sequence length. We apply RNABOR for the detection of possible RNA conformational switches, and compare RNABOR with the switch detection method paRNASS. We also provide examples of how RNABOR can at times improve the accuracy of secondary structure prediction.

**Availability:** <http://bioinformatics.bc.edu/clotelab/RNABOR/>.

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## 1 INTRODUCTION

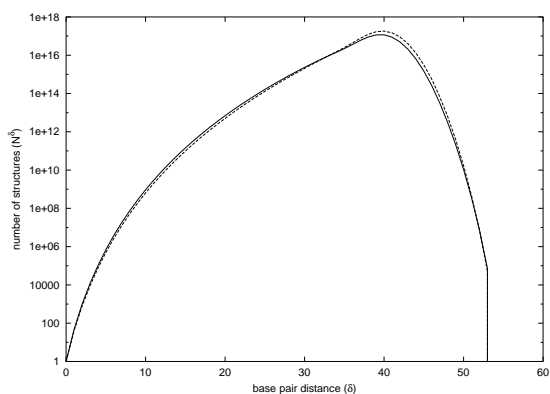
In the last few years, there has been intense interest in RNA due to the surprising, previously unsuspected roles played by ribonucleic acid in what until now has been a predominantly protein-centric view of molecular biology. Apart from its roles as messenger RNA and transfer RNA, ribonucleic acid molecules play a catalytic role in the peptidyltransferase reaction in peptide bond formation (Weinger *et al.*, 2004; Nissen *et al.*, 2000) and in intron splicing (Vicens and Cech, 2006), both examples of enzymatic RNAs now termed ribonucleic enzymes or *ribozymes* (Doudna and Cech, 2002). RNA plays a role in post-transcriptional gene regulation due to the hybridization of mRNA by small interfering RNAs (siRNA) (Harborth *et al.*, 2003; Tuschl, 2003) and microRNAs (miRNA) (Lim *et al.*, 2003). By completely different means, RNA performs transcriptional and translational gene regulation by allostery, where

a portion of the 5' untranslated region (5' UTR) of mRNA known as a *riboswitch* (Winkler *et al.*, 2002; Penchovsky and Breaker, 2005) can undergo a conformational change upon binding a specific ligand such as adenine, guanine, or lysine. RNA is known to play critical roles in various other cellular mechanisms such as dosage compensation (Brown *et al.*, 1992), protein shuttling (Walter and Blobel, 1982), expansion of the genetic code such as selenocysteine insertion (Commans and Böck, 1999), and ribosomal frameshift (Bekaert *et al.*, 2003; Moon *et al.*, 2004). Illustrative of the growing recognition for the importance of RNA, the 2006 Nobel Prize in Physiology or Medicine was awarded to A.Z. Fire and C.C. Mello for their discovery of RNA interference and gene silencing by double-stranded RNA.

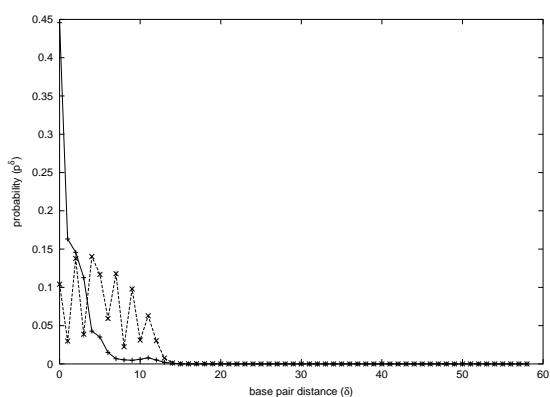
In this paper, we develop novel and efficient algorithms to investigate structures in a neighborhood of a given secondary structure  $S$  of an RNA sequence  $s$ . We call another secondary structure  $T$  of  $s$  a  $\delta$ -neighbor of  $S$ , if  $T$  and  $S$  differ by exactly  $\delta$  base pairs (see Methods section for more details). We develop algorithms to compute the number,  $N^\delta = N^\delta(s, S)$ , the partition function,  $Z^\delta = Z^\delta(s, S) = \sum_T \exp(-E(T)/RT)$ , and the minimum free energy  $MFE^\delta = MFE^\delta(s, S)$  structure over the collection of all  $\delta$ -neighbors  $T$  of  $S$ , where  $E(T)$  denotes the energy of  $T$  with respect to the Turner nearest neighbor energy model (Xia *et al.*, 1999),  $R$  is the universal gas constant, and  $T$  is temperature in Kelvin. Our software, called RNABOR (RNA neighbor), additionally computes graphs of the probability density function  $p^\delta = Z^\delta/Z$  as a function of  $\delta$ .

RNABOR was motivated by Moulton *et al.* (2000), who suggested that the stability of a secondary structure might depend on the number of structural neighbors at varying distances from the given structure – for instance from the minimum free energy (MFE) structure. It turns out that the number of structural neighbors at varying distances is not sufficient to distinguish between structural RNA and random RNA having the same MFE structure; see Figure 1. However, we do see a distinction when computing a *weighted* count of structural neighbors, where low energy structures are more heavily weighted. Formally, this is the Boltzmann partition function with respect to all structural neighbors at a given base pair distance  $\delta$ . Figure 1 displays a density plot produced by RNABOR which clearly

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(a) Number of neighbors.



(b) Probability density plot.

**Fig. 1.** The number and probability of neighboring structures at varying distances from the MFE structure of the precursor miRNA *dme-mir-1* (AE003667.3/4813-4888) from *Drosophila melanogaster* (Adams *et al.*, 2000) (solid line) and a random RNA having the same secondary structure (dashed line). The random RNA was obtained by running `RNAinverse` (Hofacker *et al.*, 1994) with the MFE structure of *dme-mir-1* as input structure.

suggests that precursor miRNA *dme-mir-1* from *Drosophila melanogaster* (AE003667) has a single, well-defined native structure, whereas a random sequence with the same MFE structure has several alternate low energy secondary structures with different topologies.

We show that the probability density plot can be used to detect RNA conformational switches and compare `RNAbor` with the conformational switch detection program `paRNAss` (Giegerich *et al.*, 1999). In `paRNAss` a structural RNA switch is predicted by means of studying properties of the energy landscape of the RNA. Secondary structures are sampled from the structure space using `RNAsubopt` (Wuchty *et al.*, 1999) or `mfold` (Zuker, 1994). Pairwise distances are calculated between the sampled structures using two different distance measures (e.g. pairs energy barrier, morphological,

tree alignment or string edit distance). Using a standard clustering method the structures are clustered into two clusters based on the distance measures. If the RNA is a conformational switch, then it has two stable structures and hence two clusters are expected (in a multi-switch, more than two stable structures are expected). As an additional test, the consensus structure of the clusters are computed and for each sample structure the distances to the two consensus structures are plotted against each other. If the RNA is really a conformational switch, then `paRNAss` output should display two clouds of points – one near the  $x$ -axis and one near the  $y$ -axis.

Note that since `paRNAss` calls `RNAsubopt` from the Vienna RNA Package program (Hofacker, 2003), it requires a user-defined energy bound,  $E$ , in order to generate all secondary structures within  $E$  kcal/mol of the minimum free energy.

The plan for the rest of this paper is as follows. In the Methods section, we describe the algorithms for computing the number  $N^\delta$ , the Boltzmann partition function  $Z^\delta$  and the minimum free energy  $MFE^\delta$  structure over the collection of all  $\delta$ -neighbors. In the Results section, we present graphs of the the number  $N^\delta$  and the Boltzmann probability density  $p^\delta = Z^\delta/Z$  of structural neighbors, which differ by  $\delta$  base pairs from a given secondary structure. In addition, we compare the output of `RNAbor` with the conformational switch detection program `paRNAss` (Giegerich *et al.*, 1999). In the Discussion section, we conclude by presenting some possible future applications of our algorithms. Pseudocode for our implementation is presented in the supplementary material. Additional data obtained by running `RNAbor` on all SAM riboswitches from Rfam (Griffiths-Jones *et al.*, 2003) is available in the web supplement at <http://bioinformatics.bc.edu/clotelab/RNAbor/webSupplement>.

## 2 MATERIALS AND METHODS

Given an RNA nucleotide sequence  $s$ , consider a fixed secondary structure  $\mathcal{S}$  of  $s$ . In this section, we describe how to efficiently compute the number  $N^\delta$  of  $\delta$ -neighbors of  $\mathcal{S}$ , the partition function  $Z^\delta$  for  $\delta$ -neighbors, and the minimum free energy  $MFE^\delta$  together with the corresponding structure over all  $\delta$ -neighbors.  $N^\delta$ ,  $Z^\delta$  and  $MFE^\delta$  are all computed for a fixed temperature. The temperature is set to  $37^\circ C$  by default, but can be changed by the user.

### 2.1 The number of $\delta$ -neighbors of a fixed secondary structure

Let  $s = s_1, \dots, s_n$  denote an RNA sequence, i.e. a sequence of letters in the alphabet of nucleotides  $\{A, C, G, U\}$ . A secondary structure  $\mathcal{S}$  on  $s$  is a set of base pairs  $(i, j)$ , where  $1 \leq i \leq i + \theta < j \leq n$  and  $\theta \geq 0$  is an integer (corresponding to minimum hairpin loop size, which we usually set to 3), such that if  $(k, l)$  is a base pair, then  $k = i \iff l = j$  (a nucleotide is involved in at most one base pair) and  $i < k < j \iff i < l < j$  (no pseudoknots). We say that  $\mathcal{S}$  is compatible with  $s$  if for every base pair  $(i, j)$  in  $\mathcal{S}$  the pair  $s_i s_j$  is

contained in the set  $\mathbb{B} = \{\text{AU, UA, GC, CG, GU, UG}\}$  (i.e. the set of Watson-Crick base pairs together with wobbles). Given two secondary structures  $\mathcal{S}, \mathcal{T}$  on  $\mathbf{s}$ , we define the base pair distance  $d_{BP}$  between  $\mathcal{S}$  and  $\mathcal{T}$  to be the number of base pairs that they have that are not in common, i.e.

$$d_{BP}(\mathcal{S}, \mathcal{T}) = |\mathcal{S} \cup \mathcal{T}| - |\mathcal{S} \cap \mathcal{T}|. \quad (1)$$

For the rest of this section, we consider both  $\mathbf{s}$  as well as the secondary structure  $\mathcal{S}$  on  $\mathbf{s}$  to be fixed. We now provide recursions for determining the number of secondary structures  $\mathcal{T}$  compatible with  $\mathbf{s}$  that are at precisely base pair distance  $\delta$  to  $\mathcal{S}$ .

Let  $\mathcal{S}_{[i,j]}$  denote the restriction of  $\mathcal{S}$  to interval  $[i, j]$  of  $\mathbf{s}$ , that is, the set of base pairs  $\mathcal{S}_{[i,j]} = \{(k, l) : i \leq k < l \leq j, (k, l) \in \mathcal{S}\}$ . A secondary structure  $\mathcal{T}_{[i,j]}$  on  $\mathbf{s}$  is a  $\delta$ -neighbor of  $\mathcal{S}_{[i,j]}$  if  $d_{BP}(\mathcal{S}_{[i,j]}, \mathcal{T}_{[i,j]}) = \delta$ . For all  $0 \leq \delta \leq m$ , and all  $1 \leq i \leq j \leq n$ , let  $\mathbf{N}_{i,j}^\delta(\mathbf{s}, \mathcal{S})$  denote the number of secondary structures  $\mathcal{T}_{[i,j]}$  compatible with  $\mathbf{s}$  such that  $d_{BP}(\mathcal{S}_{[i,j]}, \mathcal{T}_{[i,j]}) = \delta$ . In the following we may omit the sequence  $\mathbf{s}$  and secondary structure  $\mathcal{S}$  in our notation since these are fixed. In particular, we put  $\mathbf{N}_{i,j}^\delta = \mathbf{N}_{i,j}^\delta(\mathbf{s}, \mathcal{S})$ .

$\mathbf{N}_{i,j}^\delta$  is computed recursively. The initial conditions for computing  $\mathbf{N}_{i,j}^\delta$  are given by

$$\mathbf{N}_{i,j}^0 = 1, \text{ for } i \leq j, \quad (2)$$

since the only 0-neighbor to a structure is the structure itself, and

$$\mathbf{N}_{i,j}^\delta = 0, \text{ for } \delta > 0, i \leq j \leq i + \theta, \quad (3)$$

since the empty structure is the only possible structure for a sequence shorter than  $\theta + 2$  nucleotides, and so there are no  $\delta$ -neighbors for  $\delta > 0$ . The recursion used to compute  $\mathbf{N}_{i,j}^\delta$  for  $\delta > 0$  and  $j > i + \theta$  is

$$\mathbf{N}_{i,j}^\delta = \mathbf{N}_{i,j-1}^{\delta-b_0} + \sum_{\substack{s_k s_j \in \mathbb{B}, \\ i \leq k < j}} \sum_{w+w'=\delta-b} \mathbf{N}_{i,k-1}^w \mathbf{N}_{k+1,j-1}^{w'}, \quad (4)$$

where  $b_0 = 1$  if  $j$  is base paired in  $\mathcal{S}_{[i,j]}$  and 0 otherwise, and  $b = d_{BP}(\mathcal{S}_{[i,j]}, \mathcal{S}_{[i,k-1]} \cup \mathcal{S}_{[k+1,j-1]} \cup \{(k, j)\})$ . This holds since in a secondary structure  $\mathcal{T}_{[i,j]}$  on  $[i, j]$  that is a  $\delta$ -neighbor of  $\mathcal{S}_{[i,j]}$ , either nucleotide  $j$  is unpaired in  $[i, j]$  or it is paired to a nucleotide  $k$  such that  $i \leq k < j$ . In this latter case it is enough to study the smaller sequence segments  $[i, k-1]$  and  $[k+1, j-1]$  noting that, except for  $(k, j)$ , base pairs outside of these regions are not allowed. In addition, for  $d_{BP}(\mathcal{S}_{[i,j]}, \mathcal{T}_{[i,j]}) = \delta$  to be fulfilled it is necessary for  $w + w' = \delta - b$  to hold, where  $w = d_{BP}(\mathcal{S}_{[i,k-1]}, \mathcal{T}_{[i,k-1]})$  and  $w' = d_{BP}(\mathcal{S}_{[k+1,j-1]}, \mathcal{T}_{[k+1,j-1]})$ , since  $b$  is the number of base pairs that differ between  $\mathcal{S}_{[i,j]}$  and a structure  $\mathcal{T}_{[i,j]}$ , due to the introduction of the base pair  $(k, j)$ .

Pseudocode for computing  $\mathbf{N}_{i,j}^\delta$  for values of  $\delta$  between 0 and  $m$  is given in the supplementary material. The algorithm runs in time  $O(mn^3)$  and space  $O(mn^2)$  where, as defined above,  $n$  is the length of  $\mathbf{s}$  and  $m$  is the maximum value of  $\delta$ .

## 2.2 Probability analogue

In this section, we explain how to extend our approach of computing  $\mathbf{N}_{i,j}^\delta$  to compute the partition function contribution of the set of structures compatible with a given RNA sequence  $\mathbf{s}$  at a fixed base pair distance  $\delta$  from an RNA structure  $\mathcal{S}$  compatible with  $\mathbf{s}$ . This allows us to compute the probability of the set of structures compatible with  $\mathbf{s}$  at distance  $\delta$  from  $\mathcal{S}$ .

It is straight-forward to extend the previous approach to compute partition functions for the Nussinov-Jacobson energy model (Nussinov and Jacobson, 1980). In particular, by simply replacing recursion (4) with

$$\mathbf{N}_{i,j}^\delta = \mathbf{N}_{i,j-1}^{\delta-b_0} + \sum_{\substack{s_k s_j \in \mathbb{B}, \\ i \leq k < j}} \left( e^{-\frac{E_{(k,j)}}{RT}} \sum_{w+w'=\delta-b} \mathbf{N}_{i,k-1}^w \mathbf{N}_{k+1,j-1}^{w'} \right), \quad (5)$$

where  $E_{(k,j)}$  is the energy of the base pair  $(k, j)$ ,  $R$  is the gas constant, and  $T$  is the temperature, we can compute the partition function contribution of structures at a given base pair distance  $\delta$ . The base pair energy  $E_{(k,j)}$  takes the value  $-1$  if  $s_k s_j \in \mathbb{B}$  and 0 otherwise. Note that the energy contribution can be altered for different base pairs (e.g.  $-3$  for GC,  $-2$  for AU and  $-1$  for GU are weights used in (Nussinov and Jacobson, 1980)).

Employing a substantially more complicated algorithm, similar to the dynamic programming calculation of the partition function described in (McCaskill, 1990), the partition function contributions can also be computed according to the Turner energy model. In the Turner energy model a secondary structure is decomposed into loops, as described in (Zuker and Sankoff, 1984), and the energy is computed as a sum of the energy contributions of the loops. A  $k$ -loop consists of  $k-1$  base pairs (excluding the closing base pair) and  $u$  unpaired bases. The energies of 1-loops (hairpins) and 2-loops (stacks if  $u = 0$ , bulges or interior loops if  $u > 0$ ) are based on experimental data (Mathews *et al.*, 1999; Mathews and Turner, 2002) and are dependent on  $k$  and  $u$  as well as the RNA sequence. In the Turner model the energies for multi-loops ( $k > 2$ ) are generally determined by the approximate linear model  $E_M = a + b(k-1) + cu$ , where  $a$ ,  $b$  and  $c$  are constants.

As before, from now on we regard  $\mathbf{s}$  and  $\mathcal{S}$  to be a fixed RNA sequence with compatible secondary structure  $\mathcal{S}$ . The partition function for  $\mathbf{s}$  is then defined as  $\mathbf{Z} = \sum_{\mathcal{T}} e^{-E_{\mathcal{T}}/RT}$ , where the sum is taken over all structures  $\mathcal{T}$  compatible with  $\mathbf{s}$ , and  $E_{\mathcal{T}}$  is the energy of the structure  $\mathcal{T}$ . We aim to compute the restriction  $\mathbf{Z}^\delta = \mathbf{Z}_{1,n}^\delta = \mathbf{Z}_{1,n}^\delta(\mathbf{s}, \mathcal{S})$ , that is, the sum of  $e^{-E_{\mathcal{T}}/RT}$  taken over all structures  $\mathcal{T}$  that are compatible with  $\mathbf{s}$  and at base pair distance  $\delta$  from  $\mathcal{S}$ . The probability for finding a structure at a distance  $\delta$  from  $\mathcal{S}$  is then given by  $p^\delta = \mathbf{Z}^\delta / \mathbf{Z}$ .

As with the usual McCaskill partition function calculations (McCaskill, 1990), in the dynamic programming we use three matrices  $\mathbf{Z}$ ,  $\mathbf{ZB}$  and  $\mathbf{ZM}$  for recursively computing  $\mathbf{Z}^\delta$  instead of the single matrix  $\mathbf{N}$  used for computing  $\mathbf{N}^\delta$  in the previous section. In particular, for the sequence segment  $[i, j]$  of  $\mathbf{s}$ , define  $\mathbf{Z}_{i,j}^\delta = \sum e^{-E_{\mathcal{T}_{[i,j]}}/RT}$ , where the sum is over all structures  $\mathcal{T}_{[i,j]}$  compatible with  $\mathbf{s}$  and such that

$d_{BP}(\mathcal{S}_{[i,j]}, \mathcal{T}_{[i,j]}) = \delta$ . Also, define the restricted partition function  $\mathbf{ZB}_{i,j}^\delta$  as the sum of  $e^{-E_{\mathcal{T}_{[i,j]}}/RT}$  taken over all structures  $\mathcal{T}_{[i,j]}$  such that  $(i,j) \in \mathcal{T}_{[i,j]}$ , and  $\mathbf{ZM}_{i,j}^\delta$ , which is the partition function contribution if the sequence segment  $[i,j]$  is part of a multi-loop. The matrices  $\mathbf{Z}$ ,  $\mathbf{ZB}$  and  $\mathbf{ZM}$  are filled using the following three recursions.

To compute  $\mathbf{Z}$  we use the recursions

$$\mathbf{Z}_{i,j}^\delta = \mathbf{Z}_{i,j-1}^{\delta-b_0} + \sum_{\substack{s_k, s_j \in \mathbb{B}, \\ i \leq k < j}} \left( e^{-E_d/RT} \sum_{w+w'=\delta-d_1} \mathbf{Z}_{i,k-1}^w \mathbf{ZB}_{k,j}^{w'} \right), \quad (6)$$

where  $E_d$  is the energy contribution due to dangling ends (energy contributions from single bases stacking on adjacent base pairs) and closing AU base pairs (since a non GC base pair closing a stem has a destabilizing effect), and  $d_1 = d_{BP}(\mathcal{S}_{[i,j]}, \mathcal{S}_{[i,k-1]} \cup \mathcal{S}_{[k,j]})$ . Note that the first term of this recursion corresponds to the case where  $j$  is unpaired (and hence has no energy contribution) in  $[i,j]$ . The second term includes all other structures on  $[i,j]$ . The sum is taken over all possible base pairs  $(k,j)$  with  $i \leq k < j$ . If  $(k,j)$  is a base pair the partition function for  $[k,j]$  is given by  $\mathbf{ZB}_{k,j}^{w'}$ , the partition function for  $[i,k-1]$  is given by  $\mathbf{Z}_{i,k-1}^w$ .

We compute  $\mathbf{ZB}$  using the recursion

$$\begin{aligned} \mathbf{ZB}_{i,j}^\delta &= \Delta(d_{BP}(\mathcal{S}_{[i,j]}, \{(i,j)\}) - \delta) e^{-E(i,j)/RT} \\ &+ \sum_{\substack{s_k, s_l \in \mathbb{B}, \\ i < k < l < j}} \mathbf{ZB}_{k,l}^{\delta-d_2} e^{-E(i,j,k,l)/RT} \\ &+ \sum_{\substack{s_k, s_l \in \mathbb{B}, \\ i < k < l < j}} \left( e^{-(a+b+c(j-l-1))/RT} \sum_{w+w'=\delta-d_3} \mathbf{ZM}_{i+1,k-1}^w \mathbf{ZB}_{k,l}^{w'} \right), \end{aligned} \quad (7)$$

where  $E(i,j)$  is the energy of the hairpin loop with closing base pair  $(i,j)$ ,  $E(i,j,k,l)$  is the energy of the stack, bulge or interior loop with the closing base pair  $(i,j)$  and the interior base pair  $(k,l)$ ,  $d_2 = d_{BP}(\mathcal{S}_{[i,j]}, \mathcal{S}_{[k,l]} \cup \{(i,j)\})$ , and  $d_3 = d_{BP}(\mathcal{S}_{[i,j]}, \mathcal{S}_{[i+1,k-1]} \cup \mathcal{S}_{[k,l]} \cup \{(i,j)\})$ . Here,  $\Delta(x,y)$  is the Kronecker function, which equals 1 if  $x = y$ , and else 0. Note that since the above equation computes  $\mathbf{ZB}_{i,j}^\delta$ , it follows that  $(i,j)$  forms a base pair in the neighboring structures  $\mathcal{T}_{[i,j]}$  (if this is not possible then  $\mathbf{ZB}_{i,j}^\delta = 0$ ). The first term in the recursion takes care of the case where  $(i,j)$  is the only base pair in  $[i,j]$ , i.e.  $(i,j)$  closes a hairpin loop. The second term handles the case where there is an interior loop (or a bulge or a stack) closed by  $(i,j)$  and  $(k,l)$ . The third term takes care of all the structures where  $(i,j)$  closes a multi-loop. To reduce complexity of the algorithm, the interior and bulge loop size can be limited to a maximum size of  $L$ , by requiring that  $l > j - L$  in the above recursion.

The final recursion, for computing  $\mathbf{ZM}$ , is

$$\begin{aligned} \mathbf{ZM}_{i,j}^\delta &= \mathbf{ZM}_{i,j-1}^{\delta-b_0} e^{-c/RT} \\ &+ \sum_{\substack{s_k, s_j \in \mathbb{B}, \\ i \leq k < j}} \left( \mathbf{ZB}_{k,j}^{\delta-d_4} e^{-(b+c(k-i))/RT} \right. \\ &\quad \left. + \sum_{w+w'=\delta-d_5} \mathbf{ZM}_{i,k-1}^w \mathbf{ZB}_{k,j}^{w'} e^{-b/RT} \right), \end{aligned} \quad (8)$$

where  $d_4 = d_{BP}(\mathcal{S}_{[i,j]}, \mathcal{S}_{[k,j]})$  and  $d_5 = d_{BP}(\mathcal{S}_{[i,j]}, \mathcal{S}_{[i,k-1]} \cup \mathcal{S}_{[k,j]})$ . Note that since  $\mathbf{ZM}_{i,j}^\delta$  computes the partition function contribution under the assumption that  $[i,j]$  is part of a multi-loop, there will be exactly one stem-loop structure in this region (the  $\mathbf{ZB}$  term) or more than one (the  $\mathbf{ZB-ZM}$  term).

Note that the recursions for computing the number of  $\delta$ -neighbors and the partition function analogues are non-redundant in that each structure is counted once and only once.

Pseudocode for computing  $\mathbf{Z}^\delta$  is given in the supplementary material. The complexity is the same as for computing the number of  $\delta$ -neighbors,  $O(mn^2)$  in space and  $O(mn^3)$  in time, if the size of internal loops and bulges are limited to a fixed length such as 30, following the convention of Vienna RNA Package.

### 2.3 Minimum free energy $\delta$ -neighbors

Given an RNA nucleotide sequence  $\mathbf{s}$  and secondary structure  $\mathcal{S}$ , the *minimum free energy  $\delta$ -neighbor* is that secondary structure  $\mathcal{T}$  of  $\mathbf{s}$ , which has base pair distance  $\delta$  with  $\mathcal{S}$ , and which has least free energy  $\text{MFE}^\delta$  among all structures having base pair distance  $\delta$  with  $\mathcal{S}$ . Free energy is measured according to the Turner energy model (Mathews *et al.*, 1999; Xia *et al.*, 1999), where our treatment of dangles follows that of Vienna RNA package with `-d2` option.

In this section, we describe a novel algorithm capable of computing the  $\text{MFE}^\delta$  structures, for all  $\delta$ . As in our partition function computation, the run time [resp. space requirement] to compute all  $\text{MFE}^\delta$  structures for  $\delta \leq m$  is  $O(mn^3)$  [resp.  $O(mn^2)$ ]. This algorithm is obtained from the algorithm in Section 2.2 essentially by replacing Boltzmann factor  $e^{-E(T)/RT}$  by free energy  $E(T)$  and by replacing the operations of addition [resp. multiplication] by minimization [resp. addition]. In future work, we plan to analyze the structure morphological changes in proceeding from  $\mathcal{S}$  to  $\text{MFE}^0$ ,  $\text{MFE}^1$ ,  $\text{MFE}^2$ , etc. As indicated in the Results section, such an analysis could prove useful in conformational switch detection and other applications.

Fix RNA nucleotide sequence  $\mathbf{s} = s_1, \dots, s_n$  and secondary structure  $\mathcal{S}$  of  $\mathbf{s}$ . To compute  $\text{MFE}^\delta$  we use the following recursions:

$$\begin{aligned}
\text{MFE}_{i,j}^\delta &= \min \left\{ \text{MFE}_{i,j-1}^{\delta-b_0}, \right. \\
&\quad \left. \min_{\substack{s_k, s_j \in \mathbb{B}, \\ i \leq k < j}} \min_{w+w'=\delta-d_1} \text{MFE}_{i,k-1}^w + \text{MFEB}_{k,j}^{w'} + E_d \right\} \quad (9) \\
\text{MFEB}_{i,j}^\delta &= \min \left\{ \Delta(d_{BP}(\mathcal{S}_{[i,j]}, \{(i,j)\}) - \delta)E(i,j), \right. \\
&\quad \left. \min_{\substack{s_k, s_l \in \mathbb{B}, \\ i < k < l < j}} \text{MFEB}_{k,l}^{\delta-d_2} + E(i,j,k,l), \right. \\
&\quad \left. \min_{\substack{s_k, s_l \in \mathbb{B}, \\ i < k < l < j}} \min_{w+w'=\delta-d_3} \text{MFEM}_{i+1,k-1}^w + \text{MFEB}_{k,l}^{w'} + a + b + c(j-l-1) \right\} \\
\text{MFEM}_{i,j}^\delta &= \min \left\{ \text{MFEM}_{i,j-1}^{\delta-b_0} + c, \right. \\
&\quad \left. \min_{\substack{s_k, s_j \in \mathbb{B}, \\ i \leq k < j}} \left\{ \text{MFEB}_{k,j}^{\delta-d_4} + b + c(k-i), \right. \right. \\
&\quad \left. \left. \min_{w+w'=\delta-d_5} \text{MFEM}_{i,k-1}^w + \text{MFEB}_{k,j}^{w'} + b \right\} \right\}. \quad (11)
\end{aligned}$$

Once the minimum free energy of  $\delta$ -neighbors ( $\text{MFE}^\delta$ ) is computed the corresponding minimum free energy structures can be computed by a simple traceback for each  $\text{MFE}^\delta$ .

For reasons of space, the pseudocode for computing  $\text{MFE}^\delta$  is not presented; given our previous description of  $\text{MFE}^\delta$  and the pseudocode for computing the partition function  $\mathbf{Z}^\delta$ , appearing in the supplementary material, the reader will have no difficulty to reconstruct the pseudocode for  $\text{MFE}^\delta$ .

### 3 RESULTS

In this section, we present probability density graphs for a variety of conformational switches and for some non-switches. Additional data is provided for all SAM riboswitches in our web supplement. We also compare the output of `RNAbor` with distance plots generated by the web server `paRNAss` (Giegerich *et al.*, 1999), that uses a heuristic to determine whether there appear to be two or more clusters of distinct secondary structures for a given RNA sequence. Some example are also presented that indicate that `RNAbor` can be used to provide improved secondary structure predictions as compared with the MFE structure.

#### 3.1 Detecting conformational switches

In this section, we define a *conformational switch* to be an RNA sequence which has exactly two distinct low energy secondary

structures. By *multi-switch* we mean an RNA sequence which can adopt two or more distinct low energy secondary structures. For a given RNA sequence  $\mathbf{s}$  and secondary structure  $\mathcal{S}$  of  $\mathbf{s}$ , we use `RNAbor` to compute  $p^\delta = \mathbf{Z}^\delta / \mathbf{Z}$ . Taking  $\mathcal{S}$  to be the MFE structure, or alternatively the structure determined by comparative sequence alignment (Cannone *et al.*, 2002), our intuition is that a conformational switch should display a bi-modal probability density graph.

To illustrate the behavior of a typical conformational switch we present examples of `RNAbor` output for known switches. Consider for instance the 105 nt SAM riboswitch with EMBL accession number AE016750.1/132874-132778 and sequence AACUUAUCAA GAGAAGUGGA GGGACUGGCC CAAAGAAGCU UCGGCAACAU UGUAUCAUGU GCCAAUCCCA GUAACCGAGA AGGUUAGAAG AUAAGGU. Figure 2 displays three secondary structures: the MFE structure, the  $\text{MFE}^{24}$  structure, and the native structure inferred by comparative sequence analysis of the SAM riboswitch seed multiple sequence alignment from Rfam (Griffiths-Jones *et al.*, 2003). As computed by `RNAbor`, the MFE structure has free energy of  $-28.1$  kcal/mol and the Boltzmann probability  $p^0$  is 0.11, while the  $\text{MFE}^{24}$  structure has free energy of  $-26.7$  kcal/mol and  $p^{24}$  is 0.05. Note the similarity of the  $\text{MFE}^{24}$  structure with the native structure; in particular, the apical loop regions are correctly computed. There is a second MFE structure – the  $\text{MFE}^{27}$  structure, with free energy  $-28.1$  kcal/mol. Although the Boltzmann probability  $p^{27}$  is 0.16, the maximum of  $p^\delta$  over all  $\delta$ , the  $\text{MFE}^{27}$  structure is rather different than the native structure (data not shown).

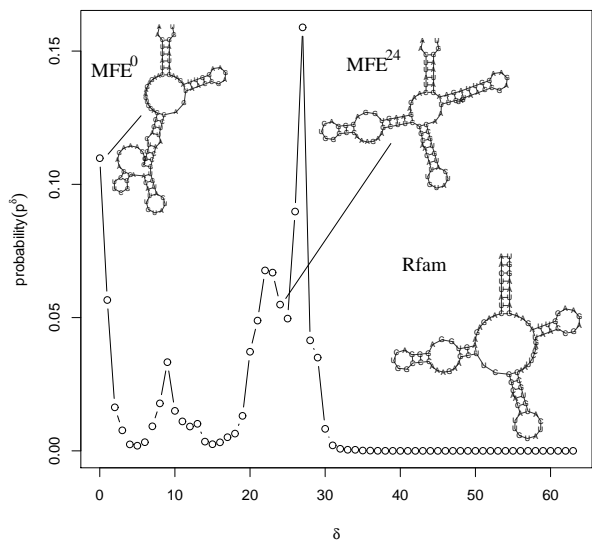
Figure 2 shows the probability density plot, i.e. the probability  $p^\delta = \mathbf{Z}^\delta / \mathbf{Z}$  of finding a structure at distance  $\delta$  from the input structure, which in this example is the MFE structure.

It is not the case that all conformational switches display a bi-modal or multi-modal Boltzmann probability density curve. In particular, the probability density curve is uni-modal for the 101 nt switch (Schlax *et al.*, 2001) with EMBL accession number AE0140031/5850-5961. This mRNA has a pseudoknotted structure, which is responsible for the translational repression of the alpha operon by an entrapment mechanism. Since the algorithm `RNAbor`, like its predecessors `mfold` and `RNAfold`, considers only non-pseudoknotted secondary structures, there is no reason to expect that `RNAbor` display a multi-modal probability density curve for this conformational switch.

Figure 3(a) depicts a bi-modal density graph for the artificially engineered bistable switch CUUAUGAGGG UACUCAUAG AGUAUCC of Flamm *et al.* (Flamm *et al.*, 2001). Figure 3(b) displays the probability density function  $p^\delta$  for the 76 nt conformational switch (Ke *et al.*, 2004), which controls hepatitis delta virus ribozyme catalysis (PDB ID 1SJ3:R). Both these examples display bi-modal Boltzmann probability curves.

#### 3.2 Comparison with paRNA<sub>ss</sub>

We now compare the ability of `RNAbor` and `paRNAss` to predict RNA conformational switches. We have chosen to display

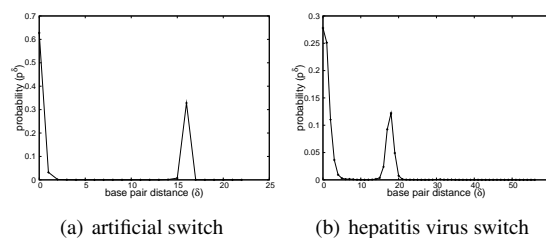


**Fig. 2.** Boltzmann probability density plot for the 105 nt SAM riboswitch with EMBL accession number AE016750.1/132874-132778. The curve shows the probability,  $p^\delta = \mathbf{Z}^\delta(\mathbf{s}, \mathcal{S})/\mathbf{Z}(\mathbf{s}, \mathcal{S})$ , for all secondary structures of RNA sequence  $\mathbf{s}$  having base pair distance  $\delta$  from the MFE structure  $\mathcal{S}$ . Alternative secondary structures for the riboswitch are shown in the figure. In the upper left is the MFE structure with free energy -28.10 kcal/mol shown, in the middle the MFE<sup>24</sup> structure with free energy -26.7 kcal/mol, and in the lower right the consensus Rfam structure. Sorted in decreasing order, the most significant Boltzmann probabilities are 0.16, 0.11, 0.090, 0.068, 0.067, 0.057, 0.055 respectively for values of  $\delta = 27, 0, 26, 22, 23, 1, 24$ .

the `paRNAss` distance plot of energy barrier versus morphological distance (Voss *et al.*, 2004), but in all the below examples the distance plots using tree alignment or string edit distance showed similar results.

The *E. coli hok* (host killing) mRNA folds into two different conformations (Franch *et al.*, 1997). The full length mRNA folds into a stable structure involving a long-range interaction between the 5' and 3'-end. Degradation of the 3'-end leads to a conformational change as the stabilizing long-range interaction is broken. Here we have investigated the part of the mRNA that undergoes a conformational change (as provided on the `paRNAss` web server <http://bibiserv.techfak.uni-bielefeld.de/parnass>).

For this RNA, both `RNAbor` and `paRNAss` detect the conformational switch, the `RNAbor` probability plot shows two distinct peaks suggesting two alternative stable structures and the `paRNAss` plot shows two clearly separated clusters, both suggesting that all the reasonably stable structures fall into one out of two conformations, see Figure 4.



**Fig. 3.** (a) Boltzmann probability density plot for the 29 nt bistable switch artificially engineered by Flamm *et al.* (2001) and having sequence CUUAUGAGGG UACUCAUAAG AGUAUCC. The graph shows the Boltzmann probability,  $p^\delta = \mathbf{Z}^\delta(\mathbf{s}, \mathcal{S})/\mathbf{Z}(\mathbf{s}, \mathcal{S})$ , of all  $\delta$ -neighbors, for all values of  $\delta$  bounded by sequence length. (b) Boltzmann probability density plot of  $\delta$ -neighbors for the 76 nt conformational switch which controls hepatitis delta virus ribozyme catalysis (PDB code 1SJ3:R) (Ke *et al.*, 2004).

Although both `RNAbor` and `paRNAss` suggest that the *hok* gene has two alternative structures, there are some uncertainties in the result. In the `RNAbor` density plot there are actually three peaks (even though the third peak is significantly smaller than the other two), indicating that there might be more than two alternative structures.

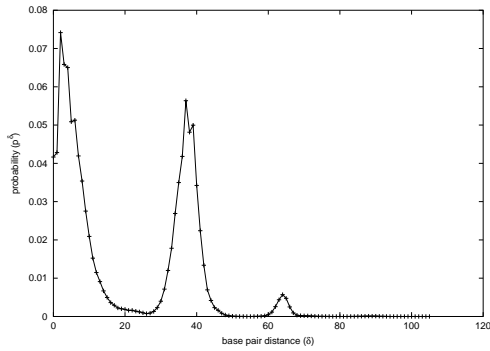
The 5'-untranslated (UTR) region of *E. coli thiM* mRNA undergoes a change in structure, that is important for regulation (Winkler *et al.*, 2002). Both `RNAbor` and `paRNAss` indicate more than one single stable structure for the *thiM*-leader. As can be seen from Figure 5 there actually seem to be more than two alternative structures. However, the third structure seems to be less important (lower probability), and hence this RNA is predicted as a conformational switch by `RNAbor`.

### 3.3 Improving on the minimum free energy structure

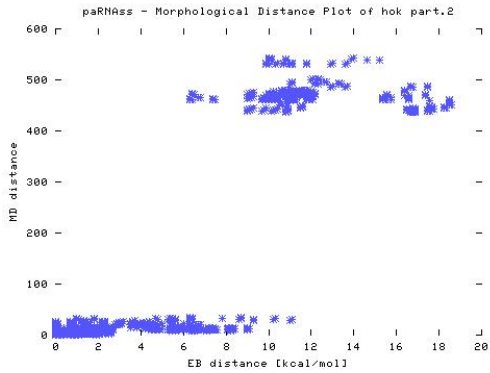
In this section, we discuss several examples where a MFE <sup>$\delta$</sup>  structure is closer to the native secondary structure, as extracted from the 3-dimensional X-ray structure, than is the MFE structure. This phenomenon generally occurs when the probability density graph indicates a second peak, although sometimes that peak may be modest.

Figure 6 present the Boltzmann probability density plot and alternate secondary structure models for the S-adenosylmethionine riboswitch mRNA regulatory element with PDB code 2GIS (Montange and Batey, 2006). The figure shows the native secondary structure for 2GIS, determined by extraction from the 3-dimensional X-ray structure<sup>1</sup>, the MFE<sup>24</sup> structure, which clearly resembles the native state, and the rather different looking MFE structure. Figure 6 graphs the probability density, where a large second peak is present, centered at  $\delta = 23$ .

<sup>1</sup> Using the software `rnview` (Yang *et al.*, 2003), we first obtained a list of all Watson-Crick cis base pairs.



(a) RNAbor density plot.



(b) paRNAss distance plot.

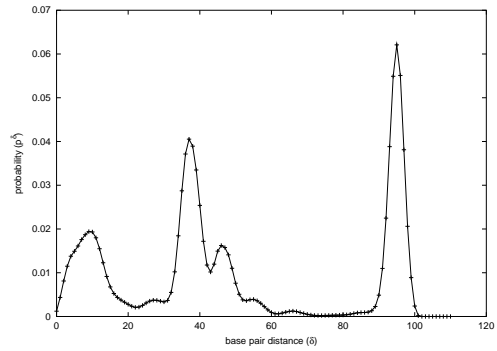
**Fig. 4.** The *E. coli hok* (*host killing*) mRNA folds into two different conformations (Franch *et al.*, 1997). (a) The RNAbor density plot shows two distinct peaks indicating that the *hok* mRNA has two alternative folds. The paRNAss (b) distance plot also indicate that this RNA sequence can fold into two alternative secondary structures.

Improvement over the MFE structure is not restricted to riboswitches. Indeed, Figure 7 displays a very unrealistic linear MFE structure for Ile-tRNA from *E. coli* – accession number D11660 from Sprinzl’s tRNA database (Sprinzl *et al.*, 1998), as well as alternative structures predicted by RNAbor. Note the correctly predicted anti-codon GAU.

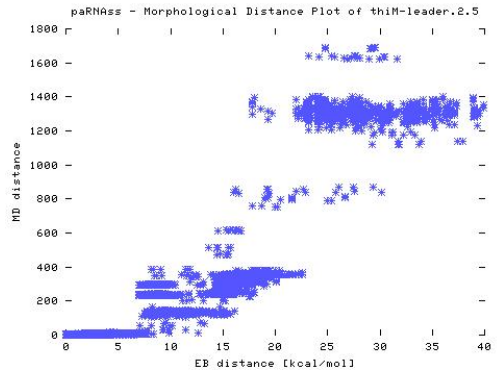
## 4 DISCUSSION

In this paper we present some novel algorithms for efficiently computing the number ( $N^\delta$ ), the Boltzmann partition function ( $Z^\delta$ ) and the minimum free energy ( $MFE^\delta$ ) and corresponding structure over the collection of all  $\delta$ -neighbors of a secondary structure of a fixed RNA sequence, all of which are implemented in the webserver RNAbor.

We find that the output of RNAbor gives useful insights into the landscape of foldings for a single RNA sequence. In addition, we observe that the output of RNAbor compares well with that of the conformational switch detection program paRNAss. In future work we will make a more extensive comparison of RNAbor with other RNA folding landscape analysis



(a) RNAbor density plot.



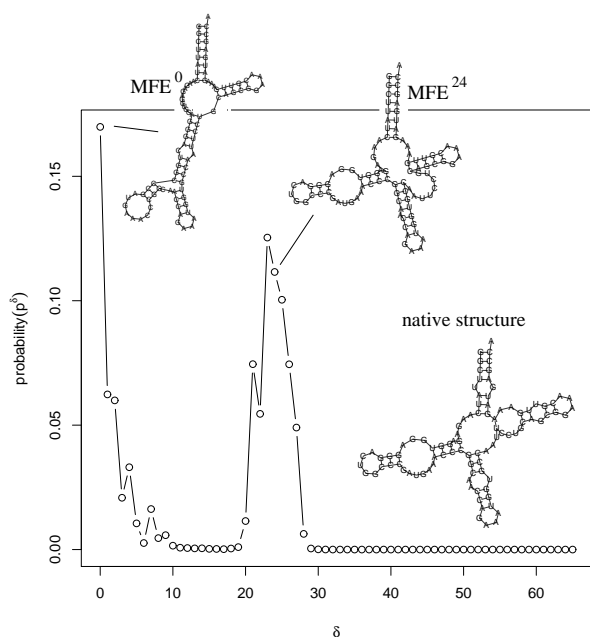
(b) The paRNAss distance plot.

**Fig. 5.** *E. coli thiM*-leader. (a) RNAbor density plot and (b) the paRNAss distance plot.

programs such as RNashapes (Giegerich *et al.*, 2004; Steffen *et al.*, 2006; Voss *et al.*, 2006) and Sfold (Ding and Lawrence, 2003; Ding *et al.*, 2004).

Potential applications of RNAbor which will be pursued in future work include the following.

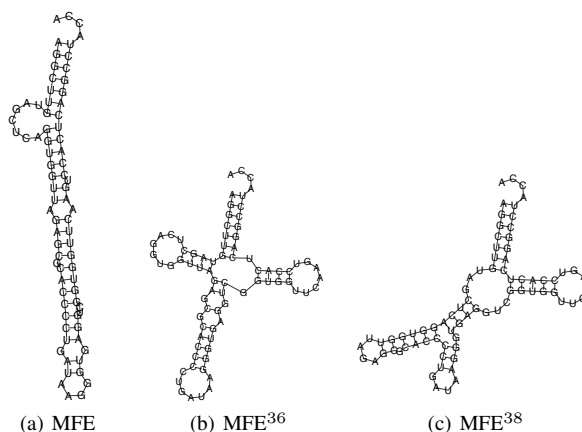
- Since RNAbor allows one to distinguish whether the given RNA nucleotide sequence  $s$  has a single pronounced *well of attraction* around a given secondary structure  $\mathcal{S}$  of  $s$ , it may be possible to use RNAbor to detect situations where the native secondary structure, as determined by X-ray crystallography, is different than that proposed by mfold and RNAfold (for example, see Section 3.3). The idea would be to determine if there is no peak around  $\delta = 0$ , when  $\mathcal{S}$  is taken to be the MFE structure.
- Figure 5(a) shows an interesting example where the RNA seems to have more than one alternative structure. Does this RNA have more than two alternative structures? Is it the case that the MFE structure is not biologically functional? (In this example, the other two alternative structures seem to be probable). Using RNAbor, we can determine the minimum free energy structures over all  $\delta$ -neighbors, and subsequently focus on  $MFE^\delta$  structures



**Fig. 6.** Boltzmann probability density plot for the S-adenosylmethionine riboswitch mRNA regulatory element, with sequence GGCUUAUCAAGAGAGGUGGAGGGACUGGCCCGAUGAAAACCGGCAACCAGAAAUGGUGCCAAUUCUGCAGCGGAAACGUUGAAAGAUGAGCCA. The MFE secondary structure, as determined by RNAfold -d2, is shown to the upper left. This structure has free energy  $-42.3$  kcal/mol, and the Boltzmann probability  $p^0 = Z^0/Z$  of the MFE structure is 0.169854. The MFE<sup>24</sup> structure computed by RNA<sub>bor</sub> for the same riboswitch sequence is shown in the middle. This structure has free energy of  $-38.8$  kcal/mol, and the Boltzmann probability  $p^{24} = Z^{24}/Z = 0.11$ . The secondary structure S-adenosylmethionine riboswitch mRNA regulatory element determined from X-ray structure 2GIS (Montange and Batey, 2006) is shown in the lower right.

where the Boltzmann probability  $p^\delta$  is high. Ultimately chemical probing experiments might determine whether these MFE <sup>$\delta$</sup>  structures are the preferred biologically active structure.

- RNA<sub>bor</sub> is a useful complement to already existing tools for detecting putative conformational switches. Unlike paRNA<sub>ss</sub>, the number of structures to be analyzed and the maximum allowable free energy difference from the MFE structure need not be decided in advance. (These can change the paRNA<sub>ss</sub> result quite dramatically). Depending on the number of structures to be analyzed and the energy bound, paRNA<sub>ss</sub> can take an exponential amount of time, in contrast to  $O(mn^3)$  time for RNA<sub>bor</sub> to compute  $N^\delta$ ,  $Z^\delta$  and MFE <sup>$\delta$</sup> .
- As shown in Figures 6 and 7, RNA<sub>bor</sub> can sometimes predict a secondary structure, which is closer to the real



**Fig. 7.** (a) Minimum free energy secondary structure, as determined by RNAfold -d2, for Ile-tRNA from *E. coli* with anti-codon GAU and accession number DI1660 from Sprinzl's tRNA database (Sprinzl *et al.*, 1998). The MFE structure has free energy of  $-28.61$  and Boltzmann probability  $p^0 = 0.136856$ . (b) MFE<sup>36</sup> structure, as determined by RNA<sub>bor</sub>. This structure has free energy of  $-26.1$  kcal/mol and  $p^{36} = 0.033946$ . (c) MFE<sup>38</sup> structure, as determined by RNA<sub>bor</sub>. This structure has free energy of  $-27.5$  kcal/mol, and  $p^{38} = 0.074037$ .

secondary structure than is the MFE structure, as determined from X-ray structures or comparative sequence analysis.

- As for any bioinformatics software, it will be necessary to perform experimental validation of predictions made by RNA<sub>bor</sub>. In future work, we intend to include user-defined constraints, which allow the user to require all investigated structures to contain certain specified base pairs and for certain specified nucleotides to remain unpaired. This will allow RNA<sub>bor</sub> to be used together with chemical probing experiments to determine biologically active conformers.

## 5 ACKNOWLEDGEMENTS

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